INT3075 Programming and Problem Solving for Mathematics

Control (Part II): Repetition



Repeating statements

- Besides selecting which statements to execute, a fundamental need in a program is repetition
 - repeat a set of statements under some conditions
- With both selection and repetition, we have the two most necessary programming statements

While and For statements

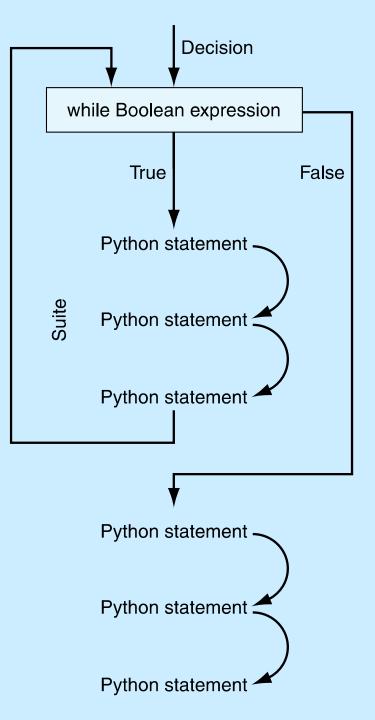
- The while statement is the more general repetition construct. It repeats a set of statements while some condition is True.
- The for statement is useful for iteration, moving through all the elements of data structure, one at a time.

while loop

- Top-tested loop (pretest)
 - test the boolean before running
 - test the boolean before each iteration of the loop

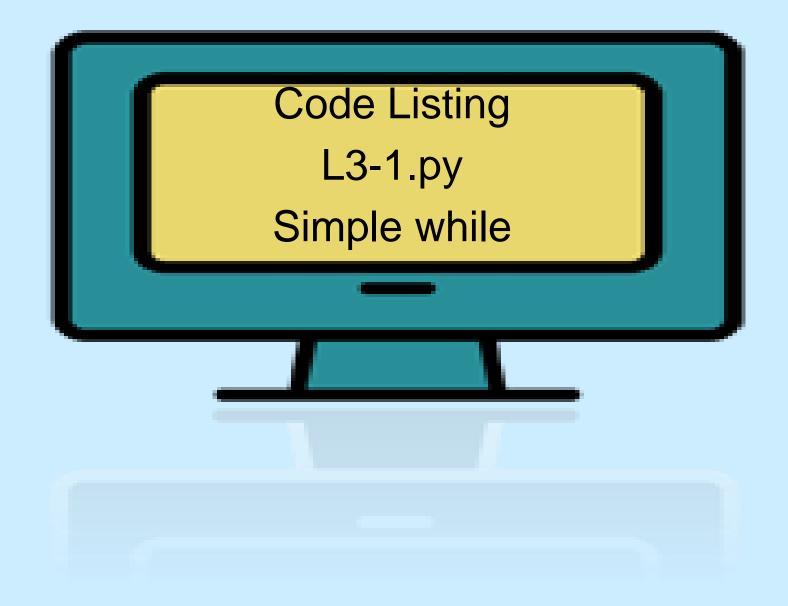
```
while boolean expression: suite
```

FIGURE 2.4 while loop.



repeat while the boolean is true

- while loop will repeat the statements in the suite while the boolean is True (or its Python equivalent)
- If the Boolean expression never changes during the course of the loop, the loop will continue forever.



```
# simple while

x_int = 0  # initialize loop—control variable

test loop—control variable at beginning of loop

while x_int < 10:

print(x_int, end=' ')  # print the value of x_int each time through the while loop

x_int = x_int + 1  # change loop—control variable

print()

print("Final value of x_int: ", x_int)  # bigger than value printed in loop!</pre>
```

General approach to a while

- outside the loop, initialize the boolean
- somewhere inside the loop you perform some operation which changes the state of the program, eventually leading to a False boolean and exiting the loop
- Have to have both!

for and iteration

- One of Python's strength's is it's rich set of built-in data structures
- The for statement iterates through each element of a collection (list, etc.)

```
for element in collection: suite
```

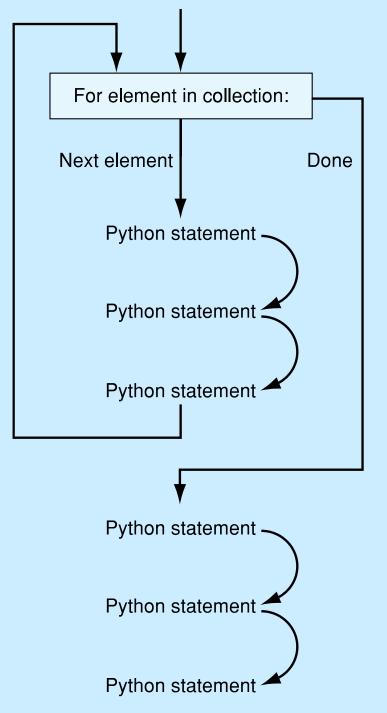
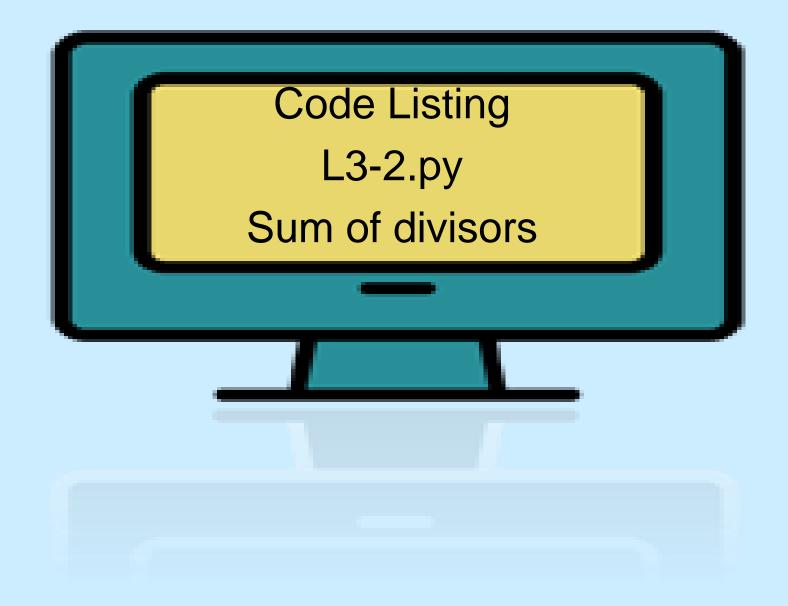


FIGURE 2.5 Operation of a for loop.



Calculate Sum of Divisors

```
divisor = 1
sum_of_divisors = 0
while divisor < number:
   if number % divisor == 0:  # divisor evenly divides theNum
       sum_of_divisors = sum_of_divisors + divisor
   divisor = divisor + 1</pre>
```

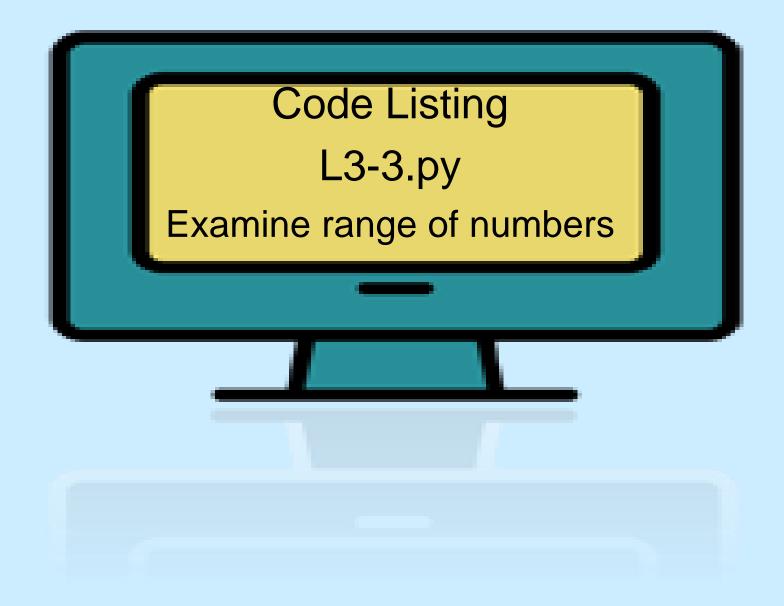
Improving the Perfect Number Program

Work with a range of numbers

For each number in the range of numbers:

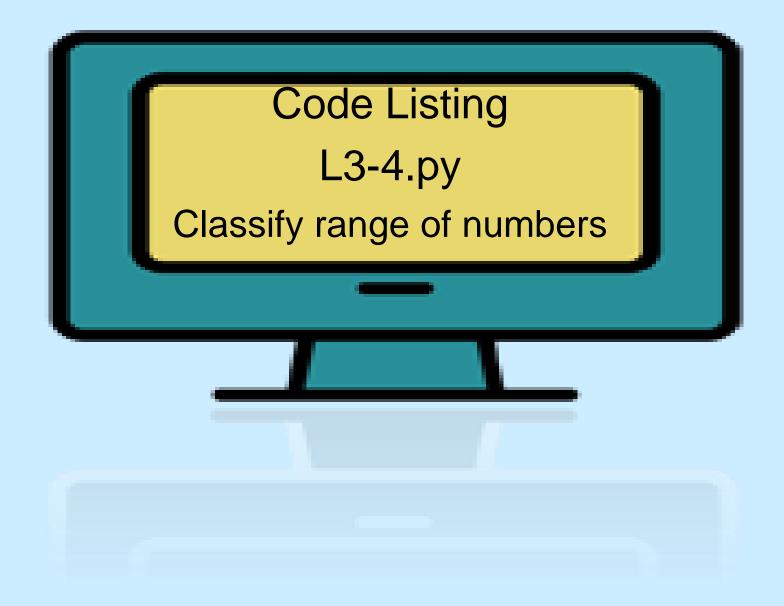
- collect all the factors
- once collected, sum up the factors
- compare the sum and the number and respond accordingly

Print a summary



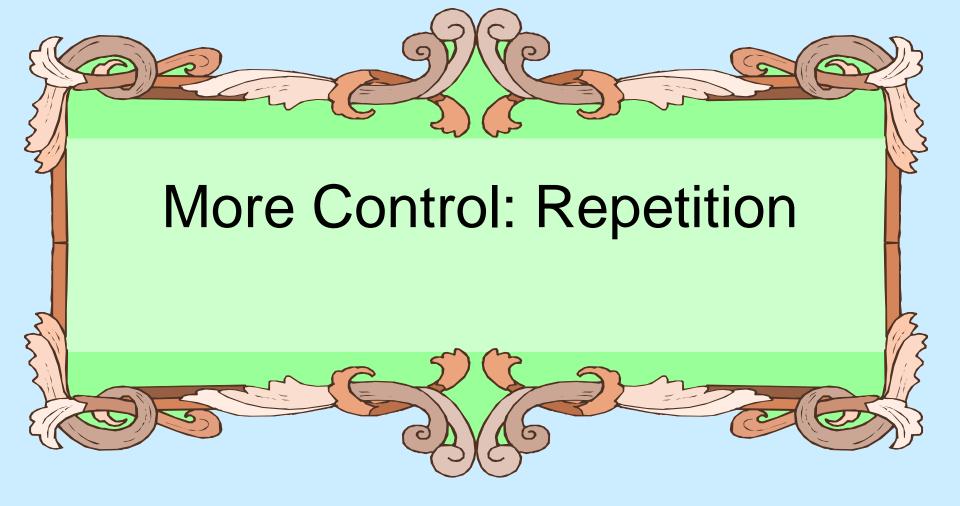
Examine a range of numbers

```
top_num_str = input("What is the upper number for the range:")
top_num = int(top_num_str)
number=2
while number <= top_num:
    # sum the divisors of number
    # classify the number based on its divisor sum
    number += 1</pre>
```



Classify range of numbers

```
# classify a range of numbers with respect to perfect, adundant or deficient
# unless otherwise stated, variables are assumed to be of type int. Rule 4
top_num_str = input("What is the upper number for the range:")
top_num = int(top_num_str)
number=2
while number <= top_num:
    # sum up the divisors
    divisor = 1
    sum of divisors = 0
    while divisor < number:
        if number % divisor == 0:
   # classify the number based on its divisor sum
   if number == sum of divisors:
       print (number, "is perfect")
   if number < sum of divisors:
       print (number, "is abundant")
   if number > sum of divisors:
       print (number, "is deficient")
   number += 1
```



Developing a while loop

Working with the *loop control variable*:

- Initialize the variable, typically outside of the loop and before the loop begins.
- •The condition statement of the while loop involves a Boolean using the variable.
- Modify the value of the control variable during the course of the loop

Issues

Loop never starts:

 the control variable is not initialized as you thought (or perhaps you don't always want it to start)

Loop never ends:

•the control variable is not modified during the loop (or not modified in a way to make the Boolean come out False)

while loop, round two

- while loop, oddly, can have an associated else suite
- else suite is executed when the loop finishes under normal conditions
 - basically the last thing the loop does as it exits

while with else

```
while booleanExpression:
 suite
 suite
else:
 suite
 suite
rest of the program
```

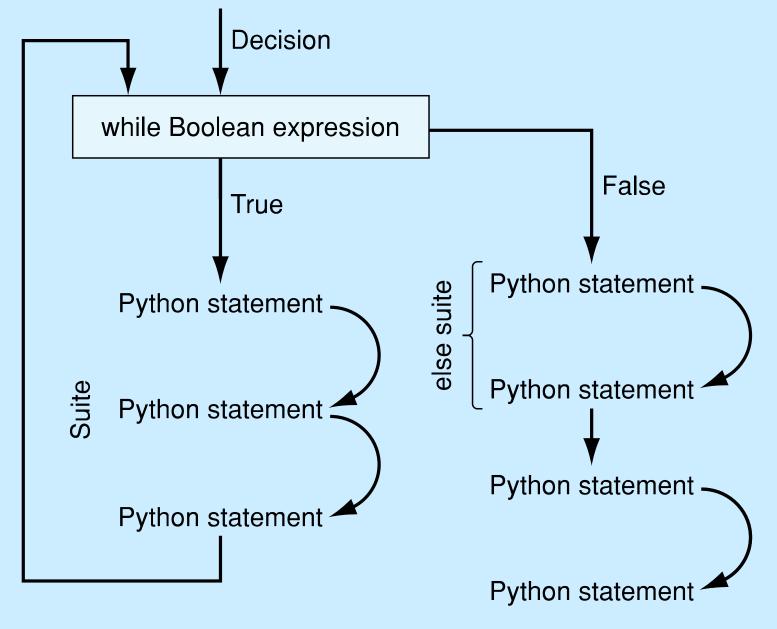


FIGURE 2.9 while-else.

Break statement

- A break statement in a loop, if executed, exits the loop
- It exists immediately, skipping whatever remains of the loop as well as the else statement (if it exists) of the loop



Hi Lo Game

```
14 # get an initial guess
15 guess_str = input("Guess a number: ")
16 guess = int(guess_str) # convert string to number
18 # while guess is range, keep asking
19 while 0 <= guess <= 100:
      if guess > number:
20
          print("Guessed Too High.")
21
      elif quess < number:
22
          print("Guessed Too Low.")
23
                            # correct guess, exit with break
  else:
24
          print("You guessed it. The number was:", number)
25
          break
26
      # keep going, get the next guess
27
      guess_str = input("Guess a number: ")
28
      guess = int(guess_str)
30 else:
      print("You quit early, the number was:", number)
31
```

Continue statement

- A continue statement, if executed in a loop, means to immediately jump back to the top of the loop and re-evaluate the conditional
- Any remaining parts of the loop are skipped for the one iteration when the continue was executed



Part of the guessing numbers program

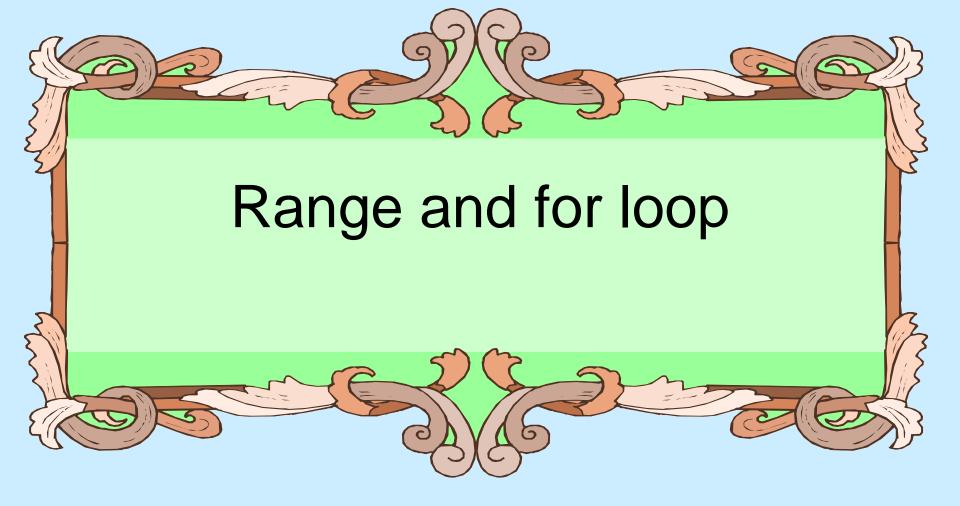
```
7 # initialize the input number and the sum
8 number_str = input("Number: ")
9 \text{ the sum} = 0
10
11 # Stop if a period (.) is entered.
12 # remember, number_str is a string until we convert it
13 while number str != "." :
     number = int(number str)
14
     if number % 2 == 1: # number is not even (it is odd)
15
          print ("Error, only even numbers please.")
16
          number_str = input("Number: ")
17
          continue # if the number is not even, ignore it
18
  the_sum += number
19
      number_str = input("Number: ")
20
21
22 print ("The sum is:",the_sum)
```

change in control: Break and Continue

- while loops are easiest read when the conditions of exit are clear
- Excessive use of continue and break within a loop suite make it more difficult to decide when the loop will exit and what parts of the suite will be executed each loop.

While overview

```
while test1:
  statement_list_1
  if test2: break
                      # Exit loop now; skip else
  if test3: continue
                      # Go to top of loop now
  # more statements
else:
  statement_list_2 # If we didn't hit a 'break'
# 'break' or 'continue' lines can appear anywhere
```



Range function

- The range function represents a sequence of integers
- the range function takes 3 arguments:
 - the beginning of the range. Assumed to be 0 if not provided
 - the end of the range, but not inclusive (up to but not including the number). Required
 - the step of the range. Assumed to be 1 if not provided
- if only one argument is provided, it is assumed to be the end value

Iterating through the sequence

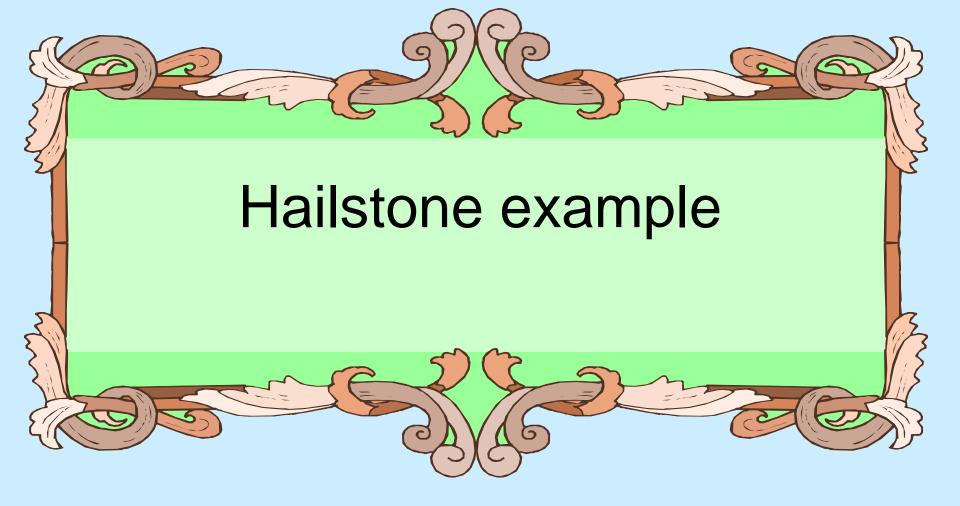
```
for num in range(1,5):
    print(num)
```

- range represents the sequence 1, 2, 3, 4
- for loop assigns num to each of the values in the sequence, one at a time, in sequence
- prints each number (one number per line)

range generates on demand

Range generates its values on demand

```
>>> range(1,10)
range(1, 10)
>>> my_range=range(1,10)
>>> type(my_range)
<class 'range'>
>>> len(my_range)
9
>>> for i in my_range:
        print(i, end=' ')
1 2 3 4 5 6 7 8 9
>>>
```



Hailstone sequence

- The Hailstone sequence is a simple algorithm applied to any positive integer
- In general, by applying this algorithm to your starting number you generate a sequence of other positive numbers, ending at 1
- Sequences go up and down just like a hailstone in a cloud

Algorithm

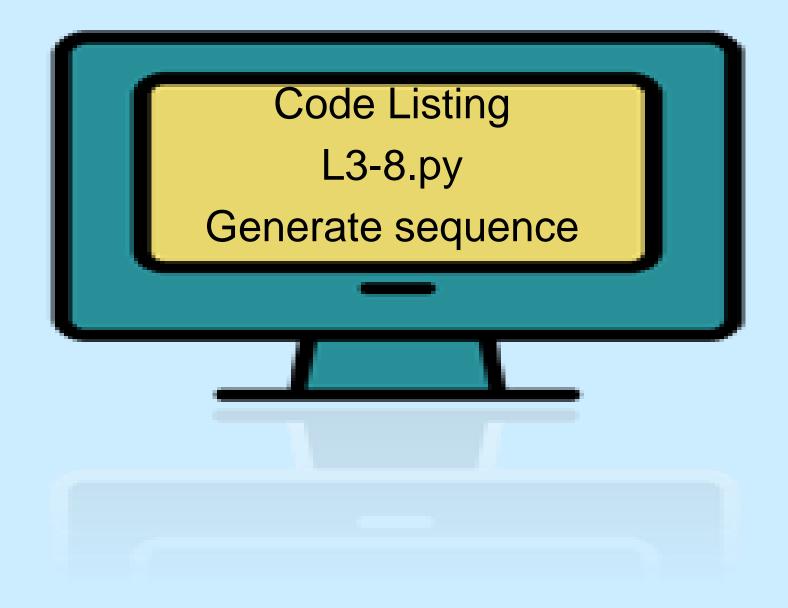
while the number does not equal one

- If the number is odd, multiply by 3 and add
 1
- If the number is even, divide by 2
- Use the new number and reapply the algorithm

Even and Odd

Use the remainder operator

```
if num % 2 == 0: # even
if num % 2 == 1: # odd
if num %2: # odd (why???)
```



```
1 # Generate a hailstone sequence
2 number_str = input("Enter a positive integer:")
3 number = int(number_str)
4 \text{ count} = 0
5
6 print("Starting with number:", number)
7 print("Sequence is: ", end=' ')
9 while number > 1: # stop when the sequence reaches 1
10
  if number%2: # number is odd
11
         number = number*3 + 1
12
                   # number is even
 else:
13
         number = number/2
14
   print(number, ", ", end=' ') # add number to sequence
15
16
   count +=1 # add to the count
17
18
19 else:
     print() # blank line for nicer output
20
     print("Sequence is ",count," numbers long")
21
```